

# Probing isocurvature perturbations with 21-cm global signal

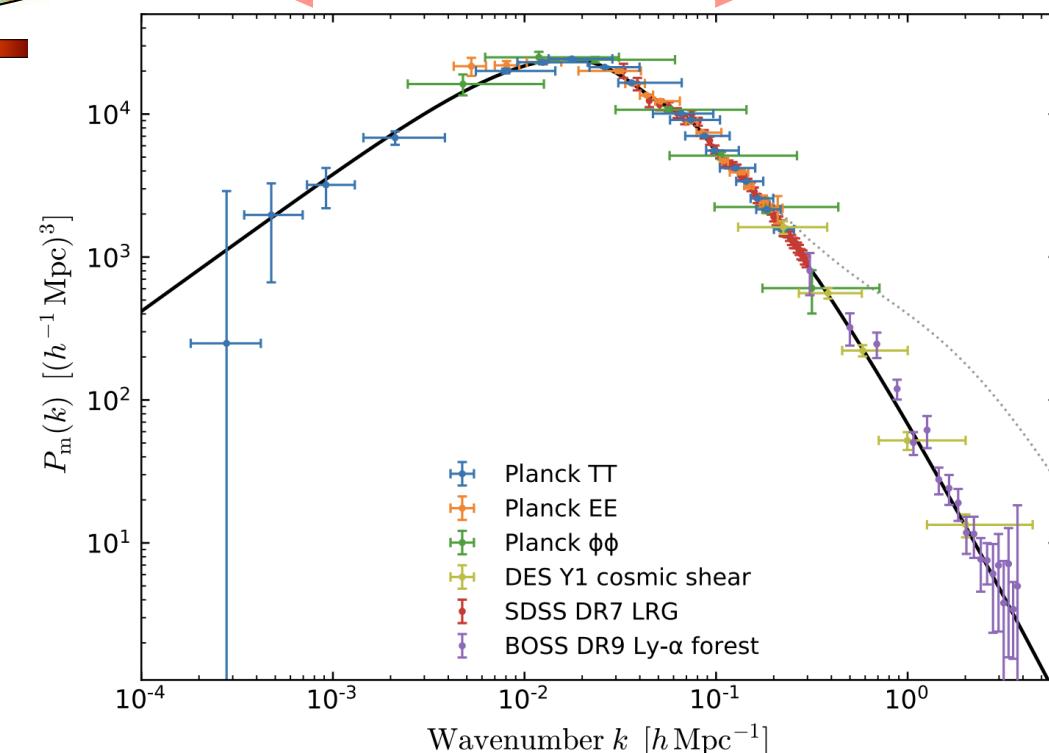
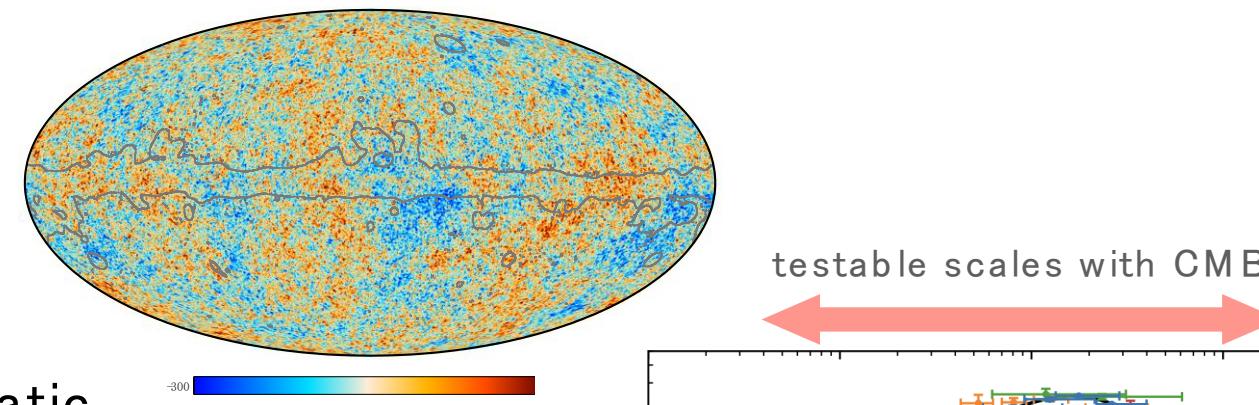
21 cm Cosmology Workshop 2024 & Tianlai Collaboration Meeting  
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(arXiv:2112.15135, PRD 105 083523)

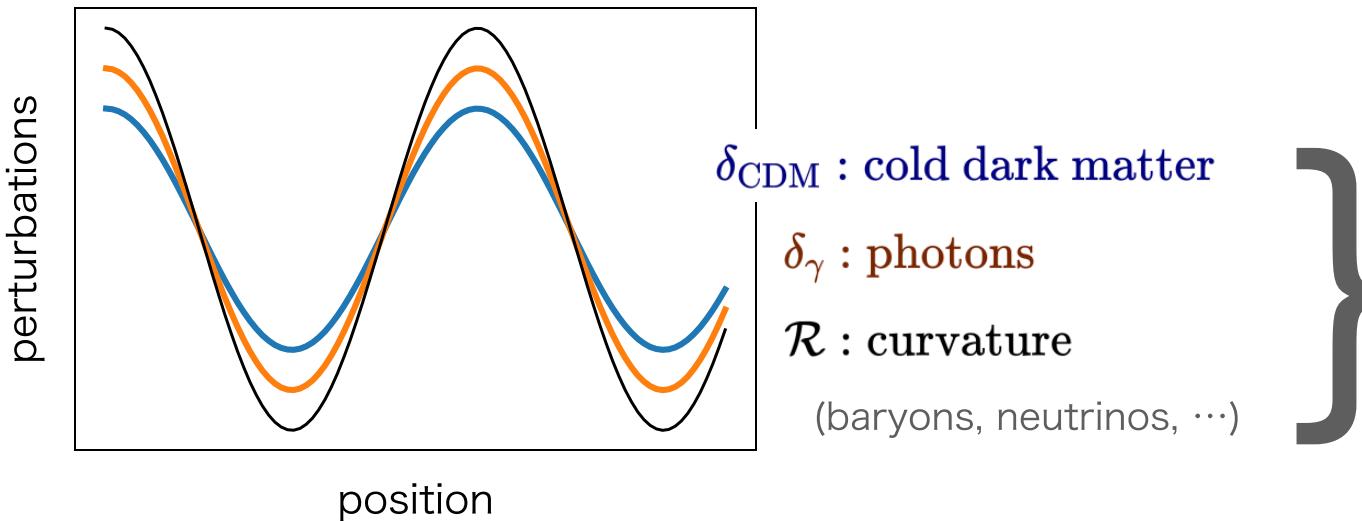
# Primordial curvature perturbations

- CMB anisotropy, galaxy distributions suggest the primordial fluctuations
- Explained very well by adiabatic (curvature) perturbations with a single power-law power spectrum
- Testable scales of primordial fluctuations with CMB are finite
- Larger scales? > Causality limit, GW ?



# Adiabatic and isocurvature perturbations

adiabatic (curvature) perturbations



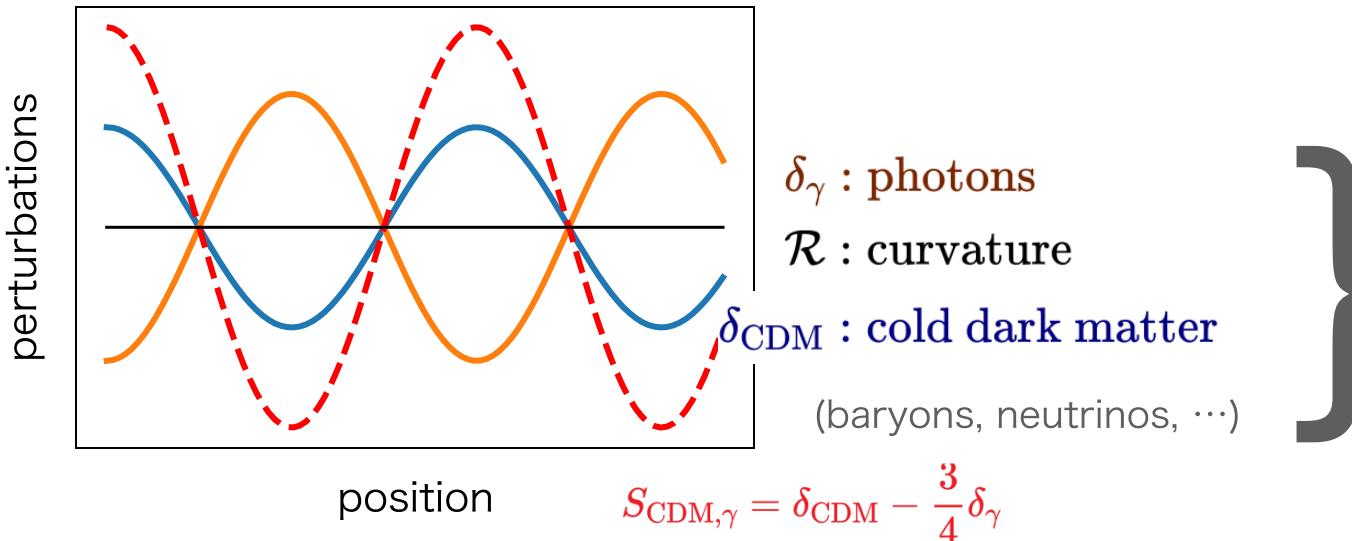
perturbations for all components have the **same** phase (and different amplitudes)

- For the pure adiabatic mode, the entropy is conserved:

$$S_{a,b} \equiv \frac{\delta n_a}{\bar{n}_a} - \frac{\delta n_b}{\bar{n}_b} = 0 \quad (n_a : \text{number density of the particle labeled "a"})$$

# Adiabatic and isocurvature perturbations

isocurvature (entropy) perturbations



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perturbations for two components have the **opposite** phase (curvature is NOT fluctuated)

- For the isocurvature mode, the entropy is perturbed:

$$S_{a,b} \equiv \frac{\delta n_a}{\bar{n}_a} - \frac{\delta n_b}{\bar{n}_b} = \frac{\delta_a}{1+w_a} - \frac{\delta_b}{1+w_b}$$

axion or PBH dark matter scenarios predict the isocurvature perturbations

# Adiabatic and isocurvature perturbations

- Power spectra of curvature and isocurvature (entropy) perturbations

$$\left. \begin{aligned} \mathcal{P}_\zeta(k) &= A_s^{\text{adi}} \left( \frac{k}{k_*} \right)^{n_s^{\text{adi}} - 1} \\ \mathcal{P}_{S_{\text{CDM}}}(k) &= A^{\text{iso}} \left( \frac{k}{k_*} \right)^{n^{\text{iso}} - 1} \\ r_{\text{CDM}} &= \frac{A^{\text{iso}}}{A_s^{\text{adi}}} \end{aligned} \right\}$$

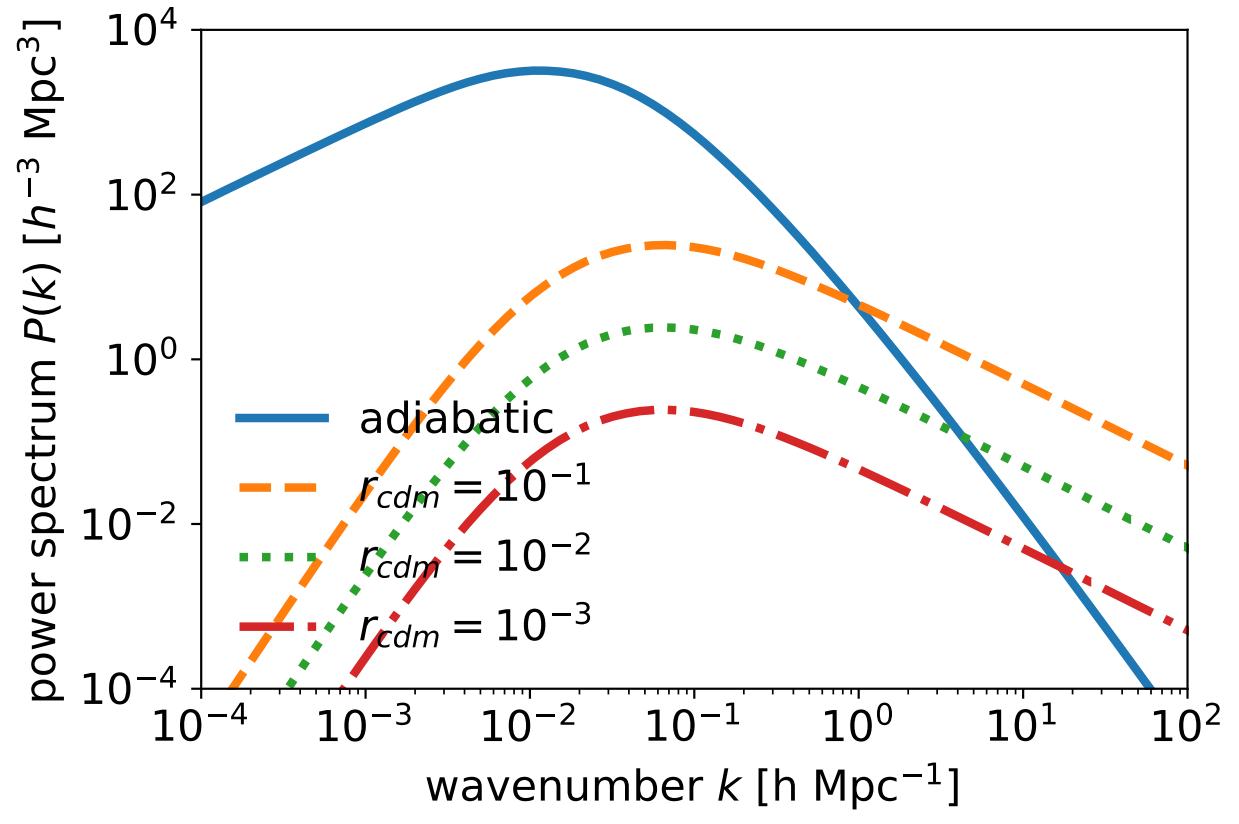
Parameters for the curvature power spectrum is fixed by Planck 2018.

$$A_s^{\text{adi}} = 2.101 \times 10^{-9}, \\ n_s^{\text{adi}} = 0.965$$

the isocurvature perturbations are parameterized by  $r_{\text{CDM}}$  and  $n^{\text{iso}}$

# Matter power spectrum

- The blue-tilted isocurvature perturbations enhance the matter power spectrum on small scales.
- Increasing  $r_{cdm}$ , the amplitude of matter power spectrum is larger.
- Blue-tilted isocurvature is expected by one of the QCD axion scenarios (Kasuya and Kawasaki 2009)



We fix  $n^{iso}=3.0$

# Astrophysical parameters

A. Mesinger, S. Furlanetto, & R. Cen (2011), MNRAS, 411, 955

- We use galaxy-driven reionization model with “21 cm FAST”
- UV luminosity function is written by:

$$\phi(M_{\text{UV}}) = \left( f_{\text{duty}} \frac{dn}{dM_h} \right) \left| \frac{dM_h}{dM_{\text{UV}}} \right|$$

- Duty cycle is parametrized by  $M_{\text{turn}}$ :

$$f_{\text{duty}} = \exp\left(-\frac{M_{\text{turn}}}{M_h}\right)$$

$M_{\text{turn}}$ : the minimum halo mass to host galaxies due to the cooling and/or stellar feedback

# Astrophysical parameters

- UV magnitude is determined by the star formation rate

$$\dot{M}_*(M_h, z) = \frac{M_*}{t_* H(z)^{-1}}$$

$t_*$  : the typical star formation timescale normalized by the Hubble time

- The stellar-to-halo mass ratio

$$\frac{M_*}{M_h} = f_{*,10} \left( \frac{M_h}{10^{10} M_\odot} \right)^{\alpha_*} \left( \frac{\Omega_b}{\Omega_m} \right)$$

# Astrophysical parameters

- The recent 21-cm observations by HERA give constraints on the astrophysical parameters

The best fitted values for HERA constraint is the model 1 (fiducial)

	$\alpha_*$	$M_{\text{turn}} [M_\odot]$	$t_*$	$\log_{10}(L_{X<2.0\text{keV}}/\text{SFR}/[\text{erg s}^{-1} M_\odot^{-1} \text{ yr}])$
model 1	0.50	$3.8 \times 10^8$	0.60	40.64
model 2	0.41	$1.6 \times 10^8$	0.29	41.52
model 3	0.62	$1.5 \times 10^9$	0.86	39.47

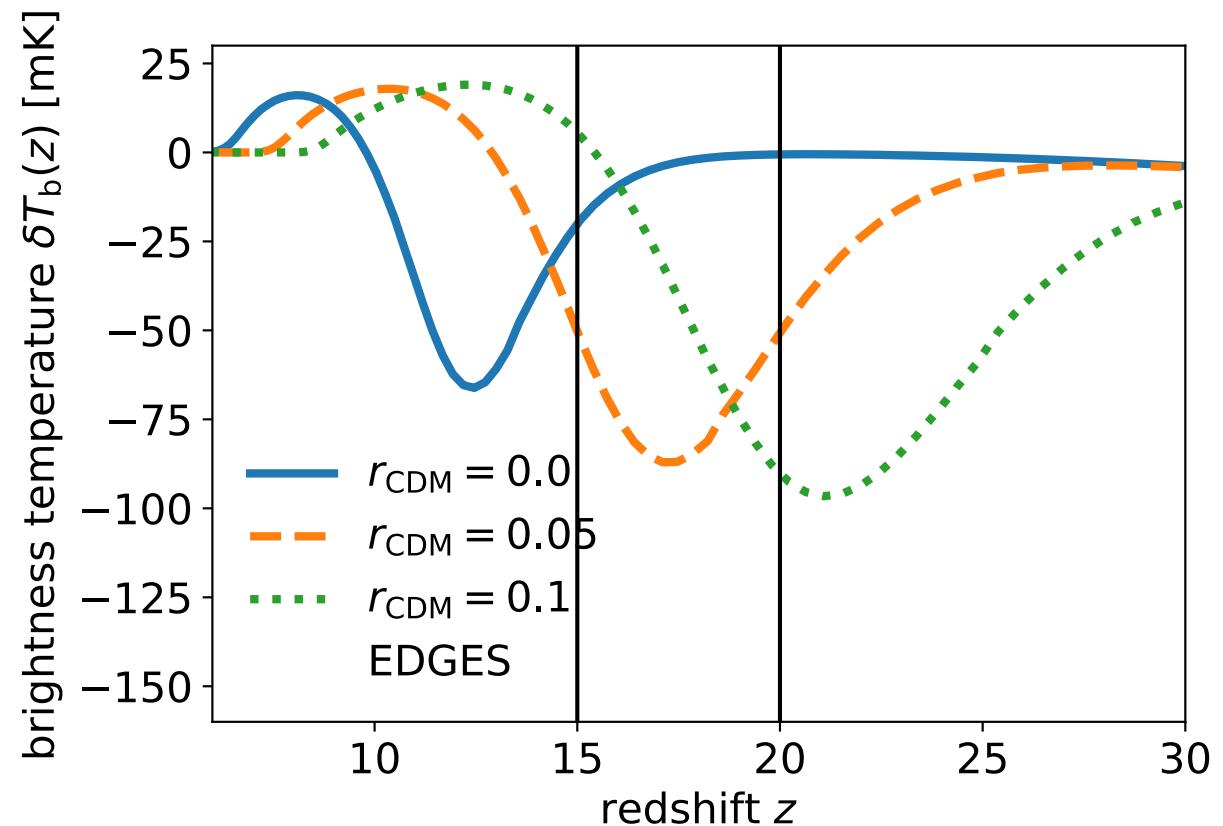
Table 1: Astrophysical parameters for each model adopted in our analysis.

# Alternative probe: 21-cm global signal

Differential brightness temperature:

$$\delta T_b(\nu) \simeq 27x_{\text{HI}}(z) \left( \frac{1+z}{10} \right)^{1/2} \left( 1 - \frac{T_{\text{CMB}}(z)}{T_{\text{spin}}(z)} \right) [\text{mK}]$$

Increasing the isocurvature fraction, the Ly- $\alpha$  coupling and heating starts at higher redshifts.



We fix  $n^{\text{iso}} = 2.5$

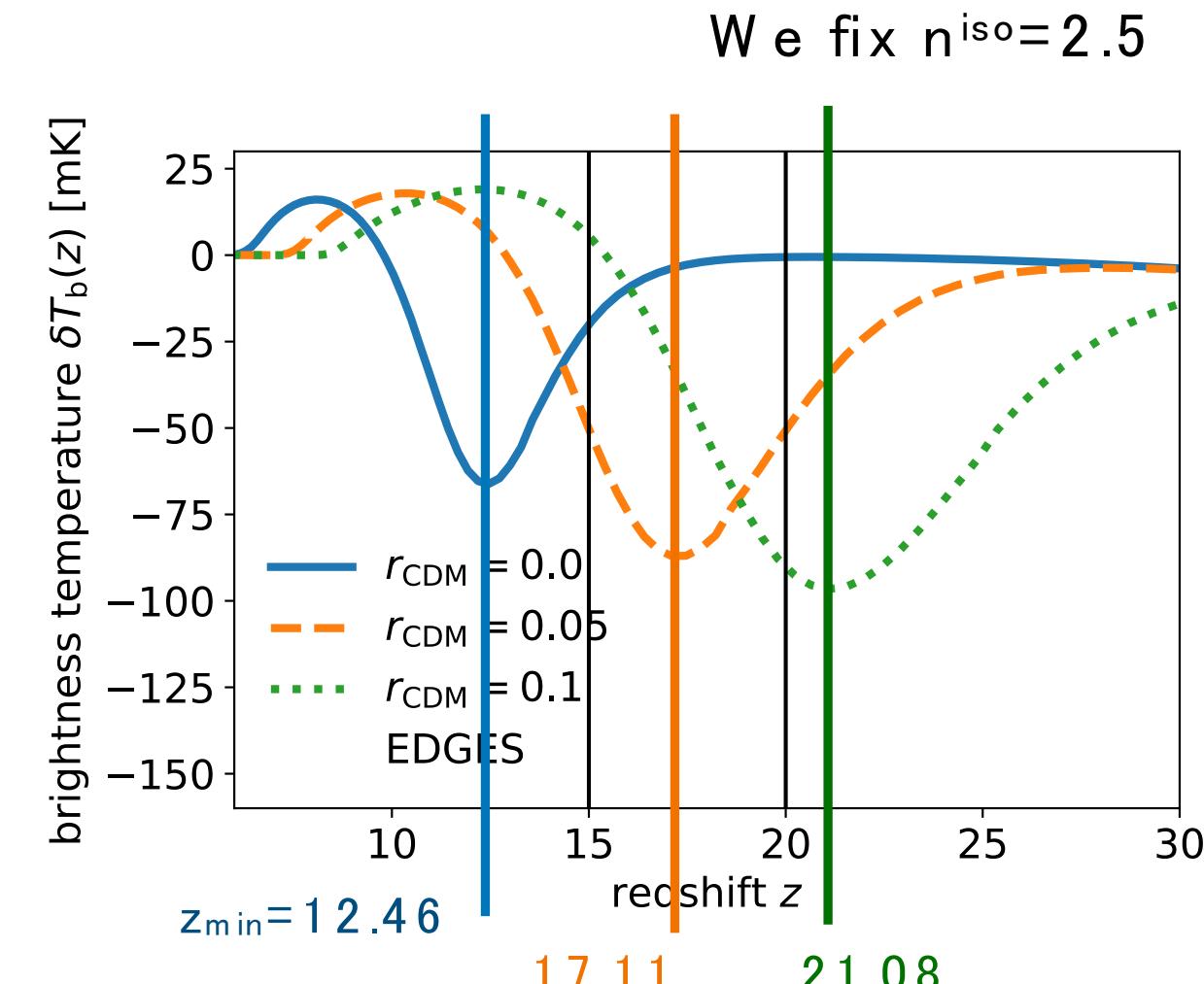
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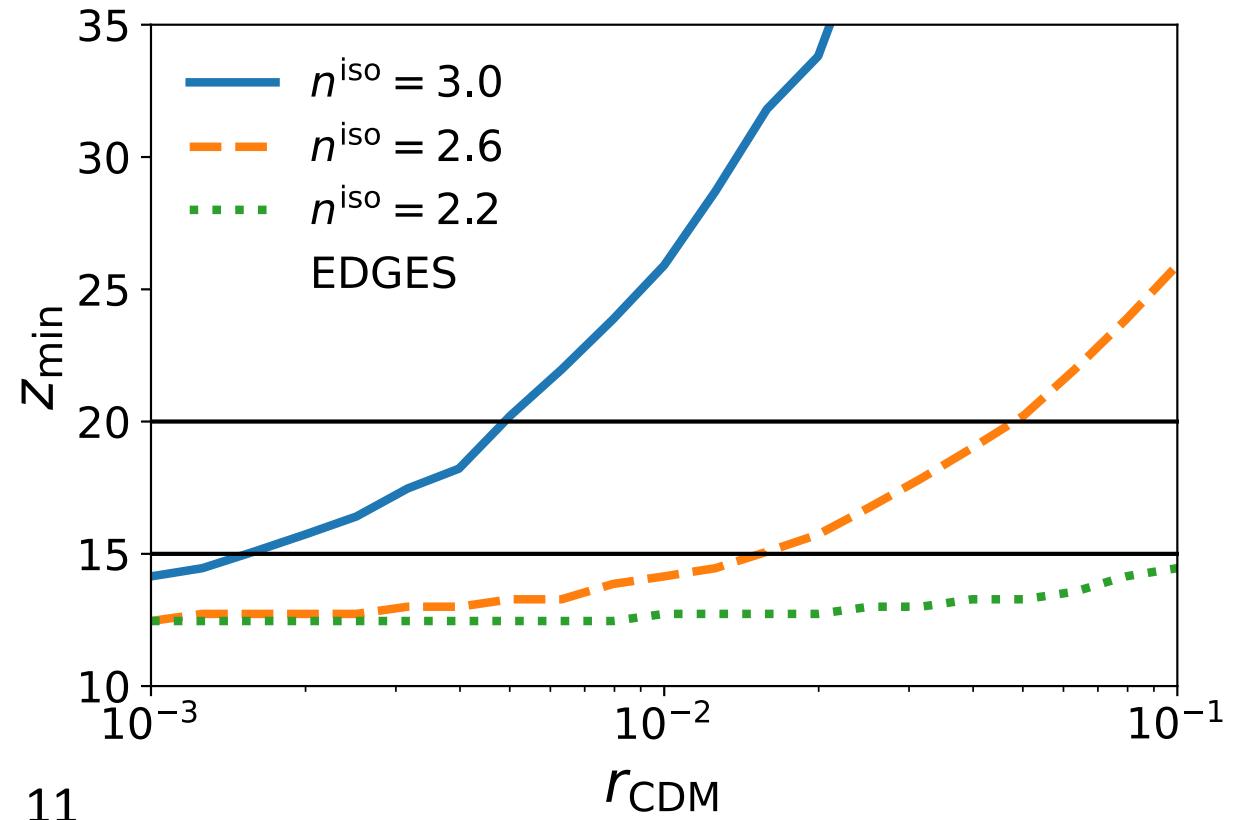
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The central redshifts of absorption signal are  $z_{\text{min}} = 12.46$  ( $r_{\text{CDM}} = 0.0$ ),  $17.11$  ( $r_{\text{CDM}} = 0.05$ ), and  $21.08$  ( $r_{\text{CDM}} = 0.1$ )



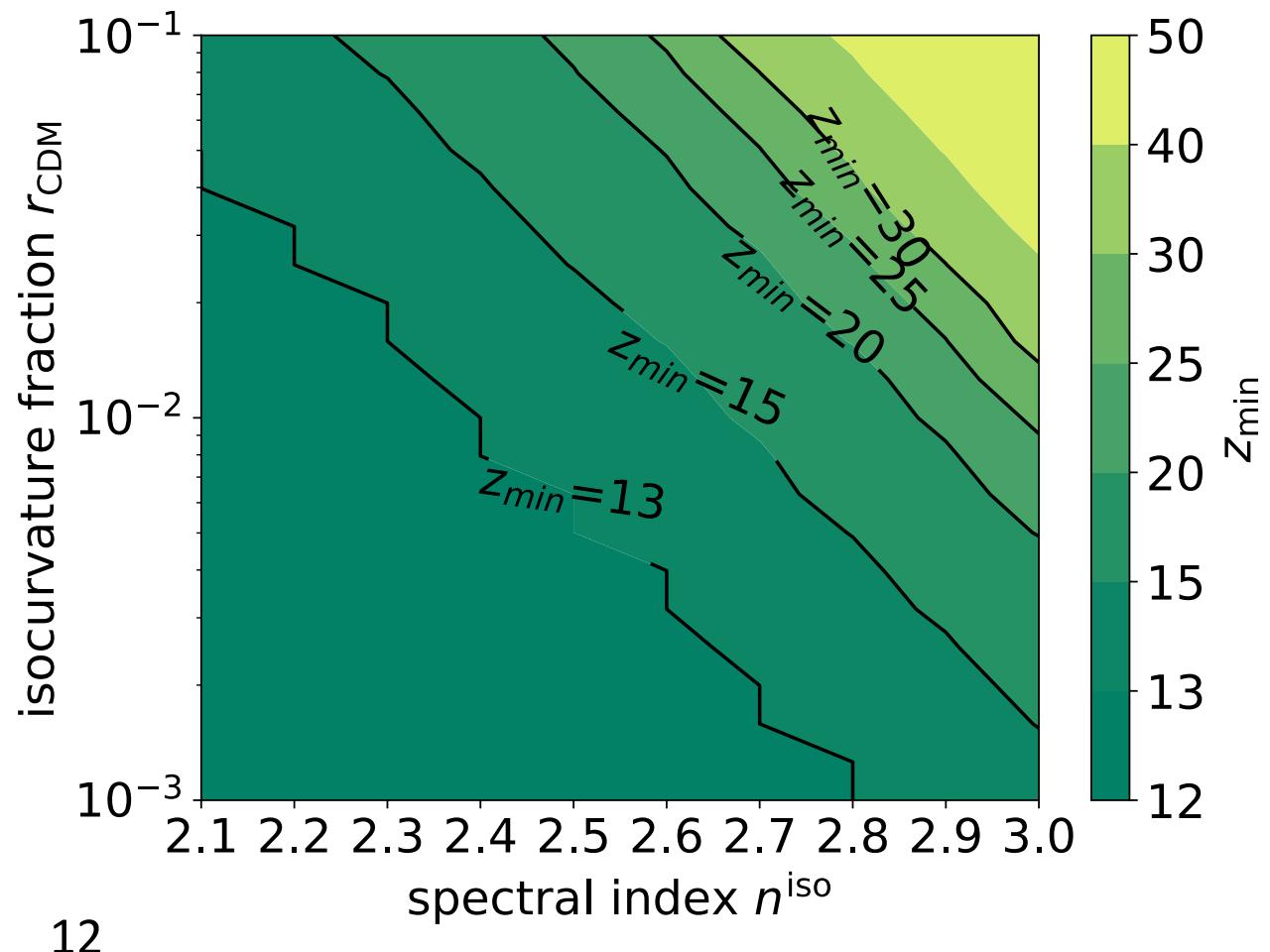
# Absorption position with varying $r_{\text{CDM}}$

- Fixing  $n^{\text{iso}}$  and increasing  $r_{\text{CDM}}$ , the central redshift of absorption gets higher.
- Fixing  $r_{\text{CDM}}$  and increasing  $n^{\text{iso}}$ , the central redshift of absorption gets higher.



# Constraints in 2-D parameter space

- Once the absorption signal can be observed around some redshift, we can obtain the constraint on the isocurvature perturbations.



# Chi<sup>2</sup> analysis in 2-D parameter space

- Calculating chi squared for different param sets,

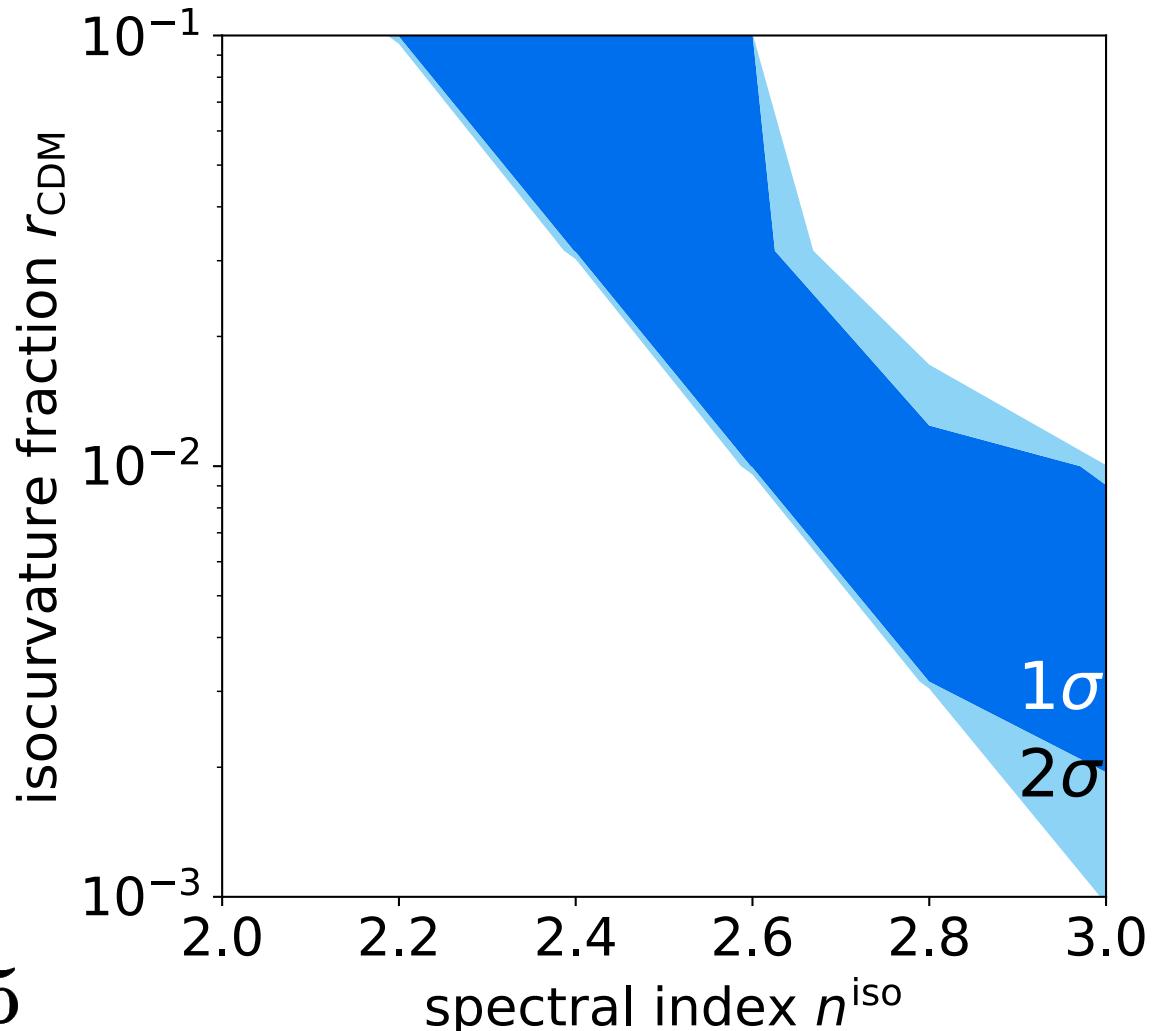
$$\mathbf{p} \equiv (r_{\text{CDM}}, n^{\text{iso}}, M_{\text{turn}}, L_{\text{X}<2.0\text{keV}}/\text{SFR})$$

$$\chi^2(\mathbf{p}) = \frac{(z_{\min,\text{th}}(\mathbf{p}) - z_{\min,\text{obs}})^2}{\Delta z_{\text{obs}}^2}$$

$$z_{\min,\text{obs}} = 17.2 \text{ and } \Delta z_{\text{obs}} = 0.2$$

- Finally the constraint is

$$4.5 \leq 2.5n^{\text{iso}} + \log_{10} r_{\text{CDM}} < 5.5$$



# Summary

- We calculate the effects of the isocurvature perturbations on the 21-cm line signal, and predict a constraint on isocurvature.
- We also discuss the degeneracy between uncertainty of astrophysical parameters and one of isocurvature parameters.
- For the future prospects, the further severe constraint would be given by the combined analysis of the 21-cm line signal and the other observables (the CMB optical depth, galaxy luminosity function, and so on)
- Please see our paper [arXiv:2112.15135](https://arxiv.org/abs/2112.15135) if you are interested